Mark Scheme (Results)

November 2021

Pearson Edexcel International GCSE In Mathematics B (4MB1)
Paper 02

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## General Marking Guidance

- All candidates must receive the same treatment. Examiners must mark the first candidate in exactly the same way as they mark the last.
- Mark schemes should be applied positively. Candidates must be rewarded for what they have shown they can do rather than penalised for omissions.
- Examiners should mark according to the mark scheme not according to their perception of where the grade boundaries may lie.
- There is no ceiling on achievement. All marks on the mark scheme should be used appropriately.
- All the marks on the mark scheme are designed to be awarded. Examiners should always award full marks if deserved, i.e. if the answer matches the mark scheme.
Examiners should also be prepared to award zero marks if the candidate's response is not worthy of credit according to the mark scheme.
- Where some judgement is required, mark schemes will provide the principles by which marks will be awarded and exemplification may be limited.
- When examiners are in doubt regarding the application of the mark scheme to a candidate's response, the team leader must be consulted.
- Crossed out work should be marked UNLESS the candidate has replaced it with an alternative response.
- Types of mark
- M marks: method marks
- A marks: accuracy marks
- B marks: unconditional accuracy marks (independent of M marks)
- Abbreviations
- cao - correct answer only
- ft - follow through
- isw - ignore subsequent working
- SC - special case
- oe - or equivalent (and appropriate)
- dep-dependent
- indep - independent
- awrt - answer which rounds to
- eeoo - each error or omission


## - No working

If no working is shown then correct answers normally score full marks

If no working is shown then incorrect (even though nearly correct) answers score no marks.

## - With working

If the final answer is wrong always check the working in the body of the script (and on any diagrams), and award any marks appropriate from the mark scheme.
If it is clear from the working that the "correct" answer has been obtained from incorrect working, award 0 marks.
If a candidate misreads a number from the question. Eg. Uses 252 instead of 255; method marks may be awarded provided the question has not been simplified. Examiners should send any instance of a suspected misread to review.
If there is a choice of methods shown, then award the lowest mark, unless the subsequent working makes clear the method that has been used.
If there is no answer achieved then check the working for any marks appropriate from the mark scheme.

## - Ignoring subsequent work

It is appropriate to ignore subsequent work when the additional work does not change the answer in a way that is inappropriate for the question: eg. Incorrect cancelling of a fraction that would otherwise be correct.
It is not appropriate to ignore subsequent work when the additional work essentially makes the answer incorrect eg algebra.
Transcription errors occur when candidates present a correct answer in working, and write it incorrectly on the answer line; mark the correct answer.

- Parts of questions

Unless allowed by the mark scheme, the marks allocated to one part of the question CANNOT be awarded to another.

| Ques | Working | Answer | Mark | Notes |
| :---: | :---: | :---: | :---: | :---: |
| 1 (a) |  |  | 3 | M1 for line $x+y=8$ correct (between $x=4$ and $x=6$ at least) Condone dashed line |
|  |  |  |  | M1 for lines $x=y$ (between $x=2$ and $x=4$ at least) and $y=2$ (between $x=2$ and $x=6$ at least) drawn correctly. Condone dashed line |
|  |  | Correct region indicated |  | A1 both method marks must be awarded. Mark the area labelled $R$. If no area is labelled allow if the area required is shaded in or out. |
| (b) |  |  | 2 | M1 for line $2 y-x=2$ drawn (between $x=2$ and $x=4$ at least) or for one correct pair of coordinates if all the given co-ordinates are on the line $y=\frac{x+2}{2} \mathrm{eg}(3,2.5)$ or $(5,3.5)$ or $(6,4)$ or $\left(\frac{14}{3}, \frac{10}{3}\right)$ |
|  |  | (2, 2), (4, 3) |  | A1 both coordinates and no extras. Condone missing brackets Allow written as $x=2, y=2$ and $x=4, y=3$ if pairing is clear. |
|  |  |  |  | Total 5 marks |



|  |  |  |  | Allow $\cos ^{-1}\left(\frac{" 10.9^{\prime 2}+" 11.3 " 2-(" \sqrt{41} ")^{2}}{2 \times " 10.9 " \times " 11.3 "}\right)$ |
| :---: | :---: | :---: | :---: | :---: |
|  |  | 33.4 |  | A1 33.4-33.5 Total 8 marks |
| 3 (a) | $(200+1) \div 2(=100.5)$ or 100th |  | 2 | M1 Allow 101 May be implied by correct answer |
|  |  | $5<t \leqslant 15$ |  | A1 Condone $\leqslant$ for < and vice versa |
| (b) | $\begin{aligned} & 2.5 \times 28+10 \times 74+25 \times 42+42.5 \times 36 \\ & +62.5 \times 20 \\ & (=70+740+1050+1530+1250 \\ & =4640) \end{aligned}$ |  | 4 | M2 for at least 3 correct products added (need not be evaluated) <br> (M1 for consistent use of a value within interval (incl end points) for at least 3 products which must be added OR correct mid-points used for at least 3 products but not added) |
|  | "4640" $\div 200$ |  |  | M1 dep on at least M1 previously scored. For dividing their sum by 200 |
|  |  | 23.2 |  | A1 (allow 23 from correct working) Allow $\frac{116}{5}$ oe |
| (c) | $\begin{aligned} & \text { FDs: } 28 \div 5(=5.6), 74 \div 10(=7.4), \\ & 42 \div 20(=2.1), 36 \div 15(=2.4), \\ & 20 \div 25(=0.8) \end{aligned}$ |  | 3 | M2 for correct methods to find at least 4 of the FD which may be on graph (M1 for at least 2 FDs which may be on graph) If there is not a scale on the $y$-axis we will allow if the bars are drawn at the correct height, in relation to the bar for $5<t \leqslant 15$ |
|  |  |  |  | A1 completely correct histogram. A correct scale with at least one correct value on the $y$-axis |
|  |  |  |  | Total 9 marks |


| 4 (a) | $0.55 \times 320(=176) \text { or } 0.45 \times 320(=144)$ oe |  | 4 | M1 Correct method to find the number of jars of jam or (honey + chutney) sold. Allow 176 or 144 seen |
| :---: | :---: | :---: | :---: | :---: |
|  | $\begin{aligned} & (320-" 176 ") \div(5+3)[=18] \text { oe or } \\ & (320-176 ") \times 3[=432] \mathrm{oe} \end{aligned}$ |  |  | M1 ft "their 176" or "their $144 "$ rather <br> than $320-" 176 "$ M2 for $\frac{3}{8} \times(320-" 176 ")$ |
|  | $" 18 " \times 3 \text { or } \frac{432 "}{8}$ |  |  | M1 ft "their 18 " or "their 432" or $\frac{3}{8} \times\left(\right.$ "144") $^{2}$ |
|  |  | 54 |  | A1 |
| (b) | $99 \times \frac{20}{9}(=220) \mathrm{oe}$ |  | 3 | M1 A correct method to find the total number of jars of jam sold on Friday |
| ( ${ }^{(220 "-2176 ") ~} \div$ "176" |  |  |  | M1 ft "their 176" or "220" - (320 - "their 144") from part(a) Allow" 176 " $\div\left(\right.$ ("220"-"176") or "220"-" 176 " $=\frac{1}{n} \times$ "176" |
|  |  | 4 |  | A1 |
| (c) | $\frac{3.50-3.20}{3.20} \times 100 \quad \text { oe }$ |  | 2 | M1 allow $\frac{3.50}{3.20}[=1.09 \ldots]$ or $\frac{3.50}{3.20} \times 100$ allow $9.4 \%$ Allow awrt 0.094 |
|  |  | 9.375 |  | A1 Allow 9.38 ISW |
| (d) | $5.10 \div 1.0625$ |  | 3 | M2 for $5.10 \div 1.0625$ oe Allow $x+0.0625 x=5.10$ <br> (M1 for $106.25 \%=5.10$ oe Allow $x+6.25 \% x=5.10$ ) |
|  |  | $\begin{gathered} \hline 4.8(0) \\ \text { (euros) } \end{gathered}$ |  | A1 Must not come from incorrect working. |
|  |  |  |  | Total 12 marks |





| 6 (a) |  | $(-4,3)$ | 2 | B2 (B1 for one correct coordinate or for $(3,-4)$ or for $\binom{-4}{3}$ ) Allow $x=-4 \quad y=3$ |
| :---: | :---: | :---: | :---: | :---: |
| (b) | $\begin{aligned} & {[A B / C D=]} \\ & \sqrt{(5--7)^{2}+(4--1)^{2}} / \sqrt{(" 8 "-"-4 ")^{2}+(" 8 "-" 3 ")^{2}}(=13) \\ & {[A C=] \sqrt{("-4 "-5)^{2}+(" 3 "-4)^{2}}=(\sqrt{82}=9.05 \ldots)} \\ & {[B D=]} \\ & \sqrt{(" 8 "--7)^{2}+\left(" 8^{\prime \prime}--1\right)^{2}}(=\sqrt{306}=3 \sqrt{34}=17.49 \ldots) \end{aligned}$ |  | 5 | M2 for 2 of these oe Correct method seen (ft through their coordinates of $C$ and $D("-4 "+12, " 3 "+5)$ )or correct answer. Ignore working if they have $[A B / C D=] 13$ <br> (M1 for correct method to find one side) Condone if not labelled <br> Alternative: <br> N.B. Alt using coordinate geometry M2 for 2 of: rectangle $=12 \times 5(=60), 0.5 \times 9 \times 1(=4.5)$, $0.5 \times(5+1) \times 3(=9), 0.5 \times 12 \times 5(=30)$ <br> ( Allow M1 for finding one of the areas) |
|  | $\begin{aligned} & \text { Eg } \cos \angle B C A=\left(\frac{" 82 "+5^{2}-" 13^{2} "}{2 \times " \sqrt{82} " \times 5}\right)\left[=\frac{-62}{10 \sqrt{82}}\right] \text { oe or } \\ & \cos \angle A B C=\left(\frac{" 13^{\prime \prime 2}+5^{2}-" 82 "}{2 \times 13 " \times 5}\right)\left[=\frac{112}{130}\right] \text { oe or } \\ & \cos \angle B A C=\left(\frac{" 82 "+" 13 " 2-5^{2}}{2 \times " 13 " \times \sqrt{82}}\right)\left[=\frac{226}{26 \sqrt{82}}\right] \text { oe } \end{aligned}$ |  |  | M1 For a correct statement, ft their lengths if clearly labelled (allow on a diagram), to enable either angle $B C A$ or angle $A B C$ or angle $B A C$ to be found or area of all 4 shapes needed to find area of shaded shape. $\angle B C A=133.2 \angle A B C=30.5 \angle B A C=16.27$ <br> Allow use of right angled triangles eg $A=90-\tan ^{-1} \frac{12}{5}-\tan ^{-1} \frac{1}{9}[=16.27 \ldots]$ |
|  | $\begin{aligned} & \text { Area of half parallelogram = } \\ & 0.5 \times 5 \times 13 " \times \sin (" 30.5 ") \\ & \text { or } 0.5 \times 5 \times 13 " \times \sin (" 149.5 \text { ") }(=16.5) \end{aligned}$ |  |  | M1 correct area formula for half parallelogram, ft their angle and sides if clearly labelled(allow on a diagram), or "60" - "30" - "9" - "4.5" (=16.5) |
|  |  | $33\left(\mathrm{~cm}^{2}\right)$ |  | A1 32.9-33 |


|  |  |  | NB: A correct answer within the given range with no obvious <br> incorrect working gains full marks. |  |
| :--- | :--- | :--- | :--- | :--- |
|  |  |  |  | Total 7 marks |

part (b) There are other ways see next page for most common
$\left.\begin{array}{|l|l|l|}\hline \begin{array}{l}\text { Alt 1 } \\ \text { (b) }\end{array} & {[A B / C D=] \sqrt{(5--7)^{2}+(4--1)^{2}}(=13)} & \\ \hline & {[\text { Line } A B] y-4=\frac{4--1}{5--7}(x-5) \text { oe }\left[\Rightarrow y=\frac{5}{12} x+\frac{23}{12}\right]} & \\ \hline & {[\text { Line } C E] y-" 3 "=-\frac{12}{5} "(x-"-4 ") \mathrm{oe}\left[\Rightarrow y=-\frac{12}{5} x-\frac{33}{5}\right]}\end{array}\right]$.

## M1 Condone not labelled

M1 Correct method to find the equation of the line. Allow use of point $B$

M1 Correct method to find the equation of the line.

M1 Correct method to find the length of $C E$ using their values for $x$ and $y$ which must be stated. If $x$ and $y$ are incorrect working must be seen


|  |  |  |  | $\pm[-5-15+28-16-21-4]$ <br> (M1 2 correct values, M2 3 correct values, M3 4 correct values) |
| :---: | :---: | :---: | :---: | :---: |
| Alt 3 |  |  |  | M4 ft their coordinates from part(a) and $D("-4 "+12, ~ " 3 "+5)$ $\pm[(-5-21-32+32)-(-28+4+24+40)]$ <br> (M1 2 correct values, M2 3 correct values, M3 4 correct values) |
|  |  |  | 33 | A1 |
| 7 (a) | $-3,1,-1,-2.38$ (allow -2.375) |  | 3 | B3 for all 4 correct values, B2 for 3 correct, B1 for 2 correct |
| (b) |  | Correct curve drawn | 3 | M1 Attempts to plot at least 7 of their points with at least 5 correct $\pm 1$ small square. (Allow if curve goes through the points) M1 drawing a smooth curve through at least 5of the plotted points. Do not allow if they use straight lines. Allow $\pm 1_{\text {square }}$ from their point. <br> A1 A fully correct curve. All Points plotted correctly, $\pm 1$ square, (allow their point $(0.5, a)$ ) provided $-2<a<-2.5$ with a smooth curve through all the points. |
| (c) |  | -1.4, -0.6, 1.9 | 2 | M1 for drawing line or showing marks on graph only at $y=0.5$ A1cao dep on M1 no incorrect extras given. |
| (d) |  |  | 2 | M1 for a tangent drawn at $x=0.5$ |
|  |  | -2 |  | A1 dep on M1 |
|  |  |  |  | Total 10 marks |



| $x$ | -2 | -1.5 | -1 | -0.5 | 0 | 0.5 | 1 | 1.5 | 2 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :--- |
| $y$ | -3 | 0.13 | 1 | 0.38 | -1 | -2.38 | -3 | -2.13 | 1 |

8 (a)
-


| 4 | B4 fully correct for all 7 correct. |
| :--- | :--- |

(NB: $x$ given in middle overlap so is not included as a correct region) Allow as numbers (ft their $x$-value)

B3 for 5 or 6 regions correct
B2 for 3 or 4 regions correct.
B1 for 2 correct regions.
NB Allow correct un-simplified expressions

|  |  |  |  | SC If using $x="$ their 17 " the max they can get is B3 B3 for 5 or 6 regions correct. B2 for 3 or 4 regions correct. B1 for 2 correct regions. |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| (b) | $24-x+x+25-x+8=40$ oe |  | 4 | M1 a correct equation for number of elements in set $C$ ft their Venn diagram, if there are no blanks, providing working is shown and the equation contains $x$ |  |
|  | $x=17$ | 17 |  | A1 |  |
|  | $\begin{aligned} & (" 17 "-2)+(21-" 17 ")+(4+\text { "17") + } \\ & (24-\text { "17") }+(\text { "17" })+(25-" 17 ")+8+25 \\ & \text { oe } \end{aligned}$ |  |  | M1 dep on M1 a correct equation using their value of $x$ ft their Venn diagram if working is shown eg $15+4+21+40+25$ or $15+4+21+7+17+8+8+25$ |  |
|  |  | 105 |  | A1 answer of 105 gets full marks |  |
|  | SC M1M1 for adding all the areas in their Venn diagram providing the $x$ 's cancel out. <br> $\operatorname{Eg}(x-2)+(21-x)+(4+x)+(25-x)+(24-x)+8+25$ oe eg $-2+21+4+25+24+8+25$ A2 for 105 |  |  |  |  |
| (c) |  | $\frac{25}{40}$ | 2 | B2 oe Allow 0.625 <br> (B1 for $\frac{n}{40}$ where $n<40$ or $\frac{25}{m}$ where $m>25$ ) |  |
|  |  |  |  | Total 10 marks |  |


| 9 | $2 r+\frac{120}{360} \times 2 \pi r=5(3+\pi)$ |  | 6 | M1 correct equation for perimeter of sector $A O D$ Allow 30.7 or better for $5(3+\pi)$ |
| :---: | :---: | :---: | :---: | :---: |
|  | $r=\frac{5(3+\pi)}{2+\frac{2}{3} \pi}[=7.5]$ |  |  | A1 correct value for $r$ - need not be simplified. Allow 30.7 or better for $5(3+\pi)$ |
|  | $\angle B O D=180-2(60-18)(=96)$ |  |  | M1 a correct method to find angle $B O D$ $\text { eg } 360-120-(180-2 \times 18) \quad \text { NB radians } \frac{8}{15} \pi$ |
|  | $\begin{aligned} & \text { Area of sector } O B C D=\frac{" 96 "}{360} \times \pi \times " 7.5^{\prime \prime 2} \\ & (=15 \pi=47.12 \ldots) \end{aligned}$ |  |  | M1 a correct method to find Area of sector $O B C D$. Ft their value of $r$ and their $\angle B O D$ eg $\pi^{" 7.55^{\prime 2}-\left(\frac{360-96}{360}\right) \times \pi " 7.5^{\prime \prime 2} 2 .}$ NB radians $\frac{1}{2} 7.5^{122} \times \frac{8}{15} \pi$ |
|  | Area of triangle $O B D=0.5 \times 7.5^{2} \times \sin " 96^{\prime \prime}$ (= 27.97...) |  |  | M1 a correct method to find the area of the triangle $O B D$ Ft their value of $r$ and their $\angle B O D$. May use trig to find lengths and use area $=0.5 \mathrm{bh}$ |
|  |  | $19.2\left(\mathrm{~cm}^{2}\right)$ |  | A1 19.1-19.2 |
|  |  |  |  | Total 6 marks |


| 10 (a) | $\begin{aligned} & \overrightarrow{A B}=6 \mathbf{b}-4 \mathbf{a} \text { oe or } \\ & \overrightarrow{B A}=4 \mathbf{a}-6 \mathbf{b} \text { oe } \end{aligned}$ |  | 3 | M1 correct vector for $\overrightarrow{A B}$ or $\overrightarrow{B A}$ May be embedded in an expression for $\overrightarrow{O C}$ |
| :---: | :---: | :---: | :---: | :---: |
|  | $\begin{aligned} & \overrightarrow{O C}=4 \mathbf{a}+\frac{3}{4}(" 6 \mathbf{b}-4 \mathbf{a} ") \text { or } \\ & \overrightarrow{O C}=6 \mathbf{b}+\frac{1}{4}(" 4 \mathbf{a}-6 \mathbf{b} ") \end{aligned}$ |  |  | M1 Allow $\overrightarrow{O C}=4 \mathbf{a}+\frac{3}{4}$ ("their $\overrightarrow{A B^{\prime}}$ ') or $\overrightarrow{O C}=6 \mathbf{b}+\frac{1}{4}$ ("their $\overrightarrow{B A^{\prime}}$ ") if $\overrightarrow{A B} / \overrightarrow{B A}$ is clearly labelled. |
|  |  | $\mathbf{a}+4.5 \mathbf{b}$ |  | A1 oe |
| (b) | $\overrightarrow{P T}=\mathbf{a}+\frac{3}{2}\left(" 6 \mathbf{b}-4 \mathbf{a}^{\prime}\right)(=-5 \mathbf{a}+9 \mathbf{b})$ |  | 4 | M1 Implied by $\frac{9}{\lambda}=\frac{-5}{-3} \mathrm{ft}$ their $\overrightarrow{A B}$ |
|  | $\begin{aligned} & \overrightarrow{P Q}=-3 \mathbf{a}+\lambda \mathbf{b} \text { or } \\ & \overrightarrow{O Q}=\lambda \mathbf{b} \text { oe } \end{aligned}$ |  |  | M1 One correct vector. Allow $\frac{6 n}{n+1}$ or $6 \lambda$ for $\lambda$ Implied by $\frac{9}{\lambda}=\frac{-5}{-3}$ |
|  $\overrightarrow{P Q}=\frac{3}{5}\left("-5 \mathbf{a}+9 \mathbf{b}^{\prime \prime}\right)(=5.4 \mathbf{b}-3 \mathbf{a})$ or <br> $\overrightarrow{O Q}=3 \mathbf{a}+\delta("-5 \mathbf{a}+9 \mathbf{b} ")$  |  |  |  | M1 A $2^{\text {nd }}$ correct vector for $P Q$ or a $2^{\text {nd }}$ correct vector for $O Q \mathrm{ft}$ their $\overrightarrow{P T}$ <br> or $5.4: 0.6$ or $\frac{9}{\lambda}=\frac{-5}{-3}$ oe $\lambda=\frac{27}{5}$ |
|  |  | 9 |  | A1 Allow 9:1 |
|  |  |  |  | Total 7 marks |






